# Contents

<table>
<thead>
<tr>
<th>Section</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>List of Videos</td>
<td>ix</td>
</tr>
<tr>
<td>Acknowledgments</td>
<td>xi</td>
</tr>
<tr>
<td>About the Authors</td>
<td>xiii</td>
</tr>
<tr>
<td>Introduction</td>
<td>1</td>
</tr>
<tr>
<td>What Works Best</td>
<td>2</td>
</tr>
<tr>
<td>What Works Best When</td>
<td>6</td>
</tr>
<tr>
<td>The Path to Assessment-Capable Visible Learners in Mathematics</td>
<td>10</td>
</tr>
<tr>
<td>How This Book Works</td>
<td>13</td>
</tr>
<tr>
<td>Chapter 1. Teaching With Clarity in Mathematics</td>
<td>17</td>
</tr>
<tr>
<td>Components of Effective Mathematics Learning</td>
<td>20</td>
</tr>
<tr>
<td>Surface, Deep, and Transfer Learning</td>
<td>21</td>
</tr>
<tr>
<td>Moving Learners Through the Phases of Learning</td>
<td>26</td>
</tr>
<tr>
<td>Surface Learning in the Secondary Mathematics Classroom</td>
<td>27</td>
</tr>
<tr>
<td>Deep Learning in the Secondary Mathematics Classroom</td>
<td>29</td>
</tr>
<tr>
<td>Transfer Learning in the Secondary Mathematics Classroom</td>
<td>29</td>
</tr>
<tr>
<td>Differentiating Tasks for Complexity and Difficulty</td>
<td>31</td>
</tr>
<tr>
<td>Approaches to Mathematics Instruction</td>
<td>33</td>
</tr>
</tbody>
</table>
Checks for Understanding
Profile of Three Teachers
  Maria Rios
  Benjamin Wittrock
  Li Shuzhen
Reflection

Chapter 2. Teaching for the Application of Concepts and Thinking Skills

Ms. Rios and Systems of Linear Equations
  What Ms. Rios Wants Her Students to Learn
  Learning Intentions and Success Criteria
  Guiding and Scaffolding Student Thinking
  Teaching for Clarity at the Close

Mr. Wittrock and Three-Dimensional Shapes
  What Mr. Wittrock Wants His Students to Learn
  Learning Intentions and Success Criteria
  Guiding and Scaffolding Student Thinking
  Modeling Strategies and Skills
  Teaching for Clarity at the Close

Ms. Shuzhen and Statistical Reasoning
  What Ms. Shuzhen Wants Her Students to Learn
  Learning Intentions and Success Criteria
  Modeling Strategies and Skills
  Teaching for Clarity at the Close

Reflection

Chapter 3. Teaching for Conceptual Understanding

Ms. Rios and Systems of Linear Equations
  What Ms. Rios Wants Her Students to Learn
  Learning Intentions and Success Criteria
  Instructional Approaches That Promote Conceptual Understanding

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Chapter 4. Teaching for Procedural Knowledge and Fluency

Ms. Rios and Systems of Linear Equations 142
   What Ms. Rios Wants Her Students to Learn 143
   Learning Intentions and Success Criteria 143
   Modeling Strategies and Skills 146
   Guiding and Scaffolding Student Thinking 149
   Instructional Approaches That Promote Procedural Knowledge 150
   Teaching for Clarity at the Close 155

Mr. Wittrock and Trigonometric Relationships 160
   What Mr. Wittrock Wants His Students to Learn 164
   Learning Intentions and Success Criteria 165
   Instructional Approaches That Promote Procedural Knowledge 166
   Teaching for Clarity at the Close 169
Ms. Shuzhen and Probabilities of Compound Events 175
What Ms. Shuzhen Wants Her Students to Learn 175
Learning Intentions and Success Criteria 176
Modeling Strategies and Skills 177
Instructional Approaches That Promote
  Procedural Knowledge 178
  Teaching for Clarity at the Close 180

Reflection 185

Chapter 5. Knowing Your Impact:
Evaluating for Mastery 187

What Is Mastery Learning? 188
  Using Learning Intentions to Define Mastery Learning 189
  Establishing the Expected Level of Mastery 190
  Collecting Evidence of Progress Toward Mastery 192

Ensuring Tasks Evaluate Mastery 201
Ensuring Tests Evaluate Mastery 204
Feedback for Mastery 207
  Task Feedback 209
  Process Feedback 210
  Self-Regulation Feedback 214

Conclusion 215
Final Reflection 218

Appendices
  A. Effect Sizes 219
  B. Teaching for Clarity Planning Guide 224
  C. Learning Intentions and Success Criteria Template 229
  D. A Selection of International Mathematical Practice or Process Standards 230

References 233
Index 235
# List of Videos

## Introduction

- Video 1: What Is Visible Learning for Mathematics?
- Video 2: Creating Assessment-Capable Visible Learners

## Chapter 1. Teaching With Clarity in Mathematics

- Video 3: What Does Teacher Clarity Mean in High School Mathematics?

## Chapter 2. Teaching for the Application of Concepts and Thinking Skills

- Video 4: Learning Intentions and Success Criteria in an Application Lesson
- Video 5: Modeling a Close Read
- Video 6: Collaborative Learning in an Application Task

## Chapter 3. Teaching for Conceptual Understanding

- Video 7: Setting the Stage for Conceptual Learning
- Video 8: Managing Student-Led Dialogic Learning
- Video 9: Making Learning Visible Through Learner Notebooks
- Video 10: Feedback Through Peer-Assisted Reflection
- Video 11: Consolidating Knowledge Through Direct/Deliberate Instruction
Chapter 4. Teaching for Procedural Knowledge and Fluency

Video 12: Differentiating Instruction to Support Surface, Deep, and Transfer Learning

Video 13: Supporting Surface Learning Needs With a Peer Tutor

Video 14: Checking for Understanding as Procedural Knowledge Deepens

Video 15: Supporting Learners’ Extension Into Transfer

Chapter 5. Knowing Your Impact: Evaluating for Mastery

Video 16: Evaluating for Mastery

Note From the Publisher: The authors have provided video and web content throughout the book that is available to you through QR (quick response) codes. To read a QR code, you must have a smartphone or tablet with a camera. We recommend that you download a QR code reader app that is made specifically for your phone or tablet brand.

Videos may also be accessed at resources.corwin.com/vlmathematics-9-12